PyLith Modeling Tutorial Computing Static Green's Functions

> Charles Williams Brad Aagaard Matthew Knepley



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- Generation of a simple graded mesh in 2D (optional)
- Generation of Green's functions in 2D and 3D
- Solution output at a specified set of points (OutputSolnPoints)
- Postprocessing of HDF5 output using h5py
- Simple linear inversion using numpy
- Plotting of inversion results using matplotlib



- Compute deformation due to unit (i.e., 1 m) slip at fault vertex for use in an inversion for fault slip
 - Slip decreases **linearly** to 0 at surrounding vertices
 - Similar but not equivalent to uniform slip over a patch (Okada dislocation)
- Provides ability to compute Green's functions with arbitrarily complex elastic structure



Green's Functions Examples

- 2-D examples: examples/2d/greensfns
 - Example components
 - Compute synthetic (fake) observations for an earthquake
 - 2 Compute displacements at sites for Green's functions
 - Invert for fault slip
 - See Section 7.15 of the PyLith User Manual
- 3-D example: examples/3d/hex8/step21
 - Limited to computing displacements at sites for Green's functions
 - No inversion



Invert for slip on reverse fault

Files are in examples/2d/greensfns/reverse

- Generate mesh using CUBIT
- Compute synthetic (fake) observations for an earthquake pylith eqsim.cfg
- Compute displacements at sites for Green's functions pylith --problem=pylith.problems.GreensFns
- Invert for fault slip See README in examples/2d/greensfns
- Visualize inversion results using matplotlib Python package See README in examples/2d/greensfns



numpy Arrays plus scientific computing tools in Python

- Similar to numerical functions in Matlab
- Included in PyLith binary distribution

h5py Python wrappers for HDF5 library

- Provides high-level access to HDF5 files
- Included in PyLith binary distribution

matplotlib 2-D plotting for Python

- Designed to be very similar to Matlab
- Not included in PyLith binary distribution
- Available from matplotlib.org



- G Green's function matrix
- d Unknown fault slip
- dapriori A priori estimate of fault slip
 - uobs Observed displacement
 - D Penalty matrix
 - θ Penalty parameter

The matrix G_{ij} gives displacement component *i* due to a unit of slip from component *j*.



Simple Linear Inversion

Original system of equations:

$$Gd = u_{obs}$$
 (1)

Augmented system of equations:

$$G_a d = u_a$$
, where $G_a = \begin{bmatrix} G \\ \theta D \end{bmatrix}$ and $u_a = \begin{bmatrix} u_{obs} \\ d_{apriori} \end{bmatrix}$ (2)

Generalized inverse:

$$G^{-g} = \left(G_a^T G_a\right)^{-1} G_a^T \tag{3}$$
$$d_{est} = G^{-g} u_a \tag{4}$$



Demonstrate computing Green's functions; no inversion

Files are in examples/3d/hex8

- Compute responses due to strike-slip and reverse slip separately
- Parameters are distributed across multiple .cfg files pylithapp.cfg General parameters for this mesh greensfns.cfg General Green's function problem settings step21.cfg Parameters specific to this example

pylith --problem=pylith.problems.GreensFns step21.cfg

