## Crustal Deformation Modeling Tutorial

Using Gravity and Initial Stresses

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### Concepts Covered in this Session

- When are gravitational stresses necessary?
- Usage of gravitational body forces in 2D
- Usage of reference stresses to balance body forces
- Usage of incompressible elasticity to achieve a reference state
- Usage of traction boundary conditions to represent a surface load



#### When Do We Need to Use Gravitational Stresses?

- Pressure/stress-dependent rheology
  - Pressure-dependent bulk rheology (e.g., plasticity)
  - Stress-dependent fault rheology (e.g., friction)
- Viscoelastic simulations where we care about vertical deformation
- Other simulations where we care about the absolute stress state



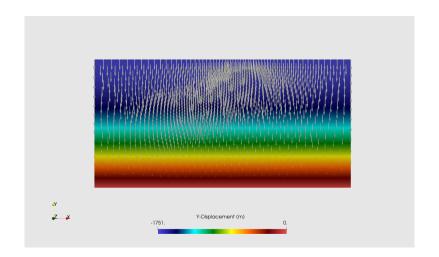
### Two-dimensional Gravity Simulations

Files are in examples/2d/reverse. None of these problems involve faulting.

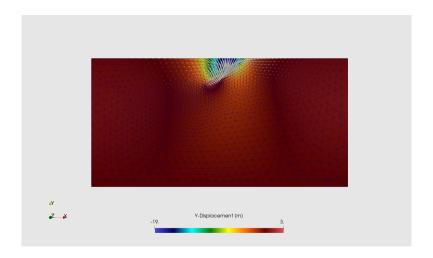
- step01 Use gravitational body forces with no reference stresses.
  - Entire domain deforms vertically since material is compressible.
- Step02 Use gravitational body forces and balance them with analytically-determined reference stresses.
  - Stresses are reasonably-well balanced and there is much less deformation.
- Step03 Use gravitational body forces for an incompressible elastic material.
  - Stresses are nearly isotropic and there is virtually no deformation.
- step04 Use traction boundary conditions to represent a surface load.
  - Primarily vertical deformation centered beneath the applied load.



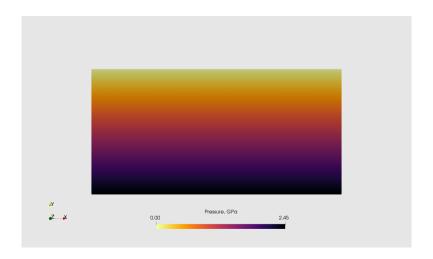
Gravitational body forces applied to elastic material



#### Gravitational body forces with reference stress



Gravitational body forces applied to incompressible elastic material



Normal tractions applied to simulate a surface load

